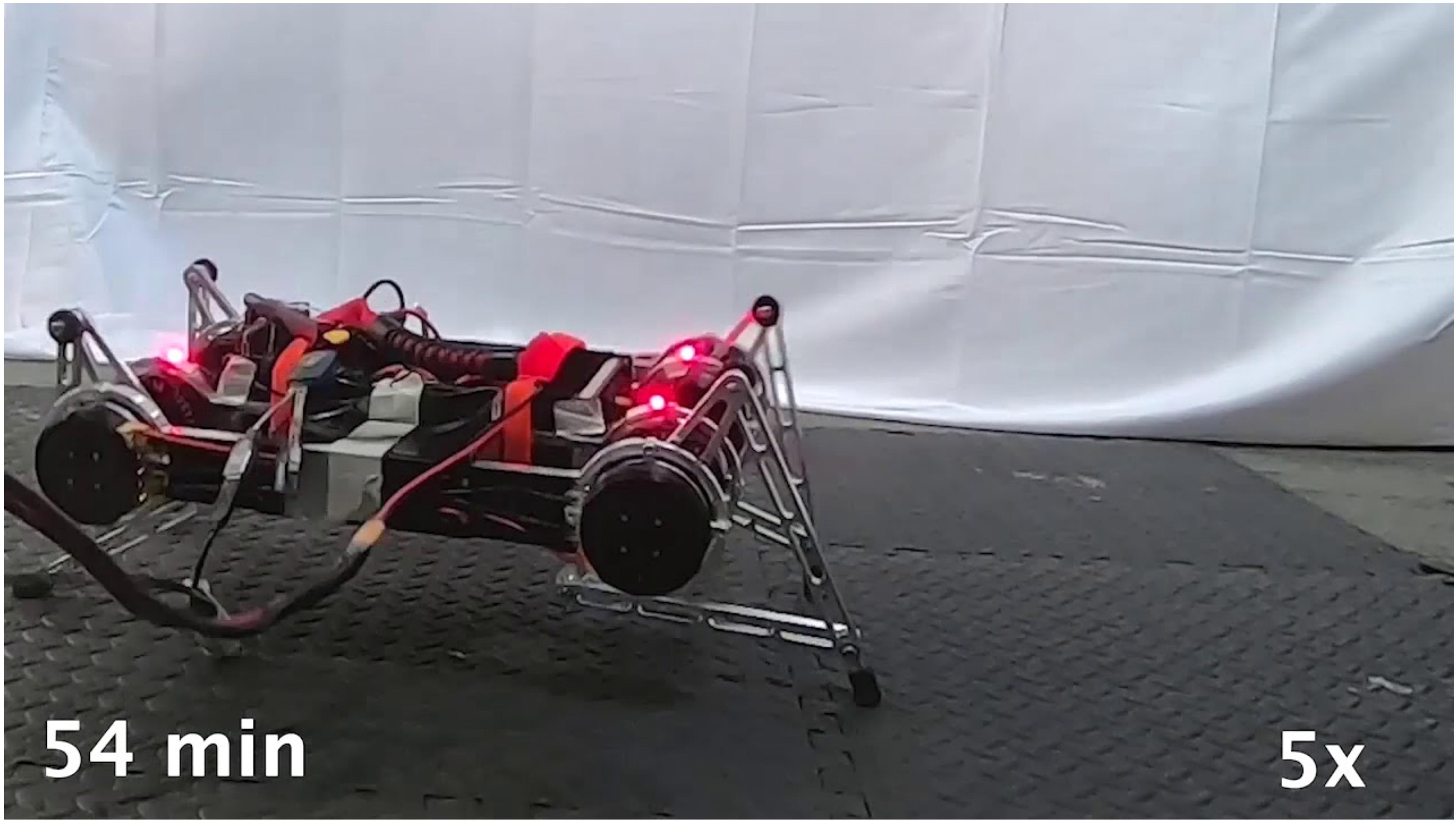


Soft Actor-Critic

Off-Policy Maximum Entropy Deep Reinforcement Learning with a Stochastic Actor

Tuomas Haarnoja Aurick Zhou Pieter Abbeel Sergey Levine

- Why Soft Actor-Critic ?
 - > sample efficient
 - > very stable
 - > exploration more efficient



54 min

5x

- Some general points:
 - actor-critic
 - off-policy algorithm
 - continuous state and action spaces

Entropy-regularized RL setting

$$H(X) = - \sum_{i=1}^n P(x_i) \log P(x_i) = -\mathbb{E} [\log P(X)]$$

$$\pi_{\text{old}}^* = \arg \max_{\pi} \mathbb{E}_{\tau \sim \pi} \left[\sum_{t=0}^{\infty} \gamma^t \left(R(s_t, a_t, s_{t+1}) \right) \right]$$

$$\pi^* = \arg \max_{\pi} \mathbb{E}_{\tau \sim \pi} \left[\sum_{t=0}^{\infty} \gamma^t \left(R(s_t, a_t, s_{t+1}) + \alpha H(\pi(\cdot | s_t)) \right) \right]$$



$$V^\pi(s_0)$$

Entropy-regularized RL setting

$$V^\pi(s) = \underset{\tau \sim \pi}{\mathbb{E}} \left[\sum_{t=0}^{\infty} \gamma^t \left(R(s_t, a_t, s_{t+1}) + \alpha H(\pi(\cdot | s_t)) \right) \mid s_0 = s \right]$$

$$Q^\pi(s, a) = \underset{\tau \sim \pi}{\mathbb{E}} \left[\sum_{t=0}^{\infty} \gamma^t R(s_t, a_t, s_{t+1}) + \alpha \sum_{t=1}^{\infty} \gamma^t H(\pi(\cdot | s_t)) \mid s_0 = s, a_0 = a \right]$$

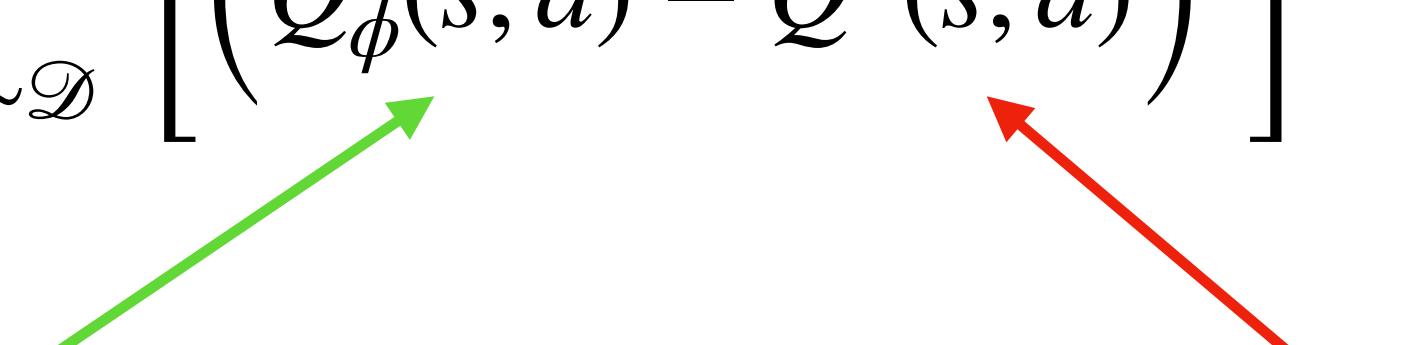
Equation de Bellman pour $Q^\pi(s, a)$:

$$Q^\pi(s, a) = \underset{\substack{s' \sim P \\ a' \sim \pi}}{\mathbb{E}} [R(s, a, s') + \gamma V^\pi(s')]$$

$$Q^\pi(s, a) = \underset{\substack{s' \sim P \\ a' \sim \pi}}{\mathbb{E}} [R(s, a, s') + \gamma (Q^\pi(s', a') + \alpha H(\pi(\cdot | s')))]$$

Critic

Loss function of the Critic: MSBE (*Mean Squared Bellman Error*)

$$L(\phi, \mathcal{D}) = \underset{(s,a,r,s',d) \sim \mathcal{D}}{\text{E}} \left[\left(Q_\phi(s, a) - Q^\pi(s, a) \right)^2 \right]$$


Critic

Loss function of the Critic: MSBE (*Mean Squared Bellman Error*)

$$L(\phi, \mathcal{D}) = \mathbb{E}_{(s,a,r,s',d) \sim \mathcal{D}} \left[(Q_\phi(s, a) - Q^\pi(s, a))^2 \right]$$


$$Q^\pi(s, a) \approx R(s, a, s') + \gamma \left(Q^\pi(s', \tilde{a}') - \alpha \log \pi(\tilde{a}' | s') \right) \quad \text{avec } \tilde{a}' \sim \pi_\theta(\cdot | s')$$

Critic

Loss function of the Critic: MSBE (*Mean Squared Bellman Error*)

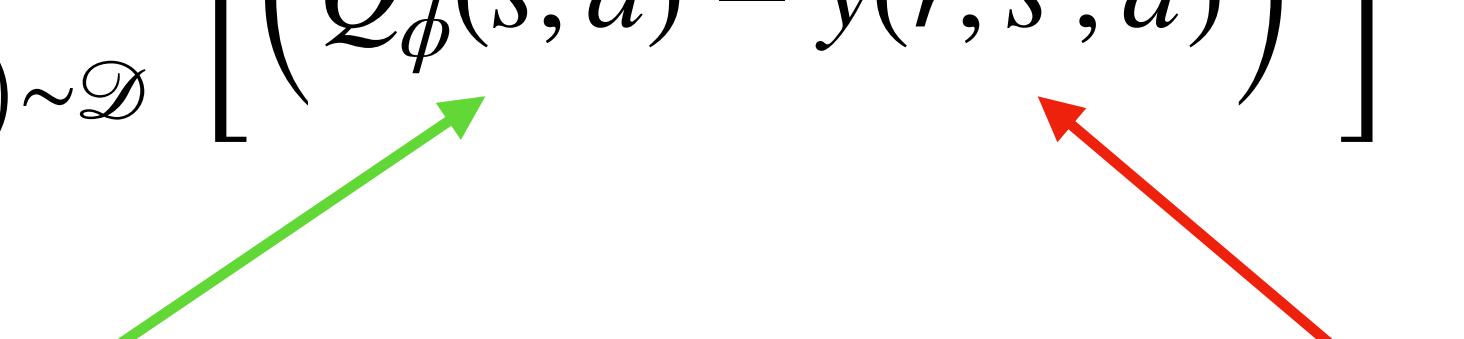
$$L(\phi, \mathcal{D}) = \underset{(s,a,r,s',d) \sim \mathcal{D}}{\text{E}} \left[\left(Q_\phi(s, a) - y(r, s', d) \right)^2 \right]$$


$$y(r, s', d) = R(s, a, s') + \gamma(1 - d)\left(Q_\phi(s', \tilde{a}') - \alpha \log \pi(\tilde{a}' | s')\right) \quad \text{avec } \tilde{a}' \sim \pi_\theta(\cdot | s')$$

Critic

1st trick: Target Networks

Loss function of the Critic: MSBE (*Mean Squared Bellman Error*)

$$L(\phi, \mathcal{D}) = \underset{(s,a,r,s',d) \sim \mathcal{D}}{\text{E}} \left[\left(Q_\phi(s, a) - y(r, s', d) \right)^2 \right]$$


$$y(r, s', d) = R(s, a, s') + \gamma(1 - d) \left(Q_{\phi_{targ}}(s', \tilde{a}') - \alpha \log \pi(\tilde{a}' | s') \right) \quad \text{avec} \quad \tilde{a}' \sim \pi_\theta(\cdot | s')$$

$$\phi_{\text{targ}} \leftarrow \rho\phi_{\text{targ}} + (1 - \rho)\phi$$

Silver, David, et al. "Deterministic policy gradient algorithms." *International conference on machine learning*. PMLR, 2014.

Critic

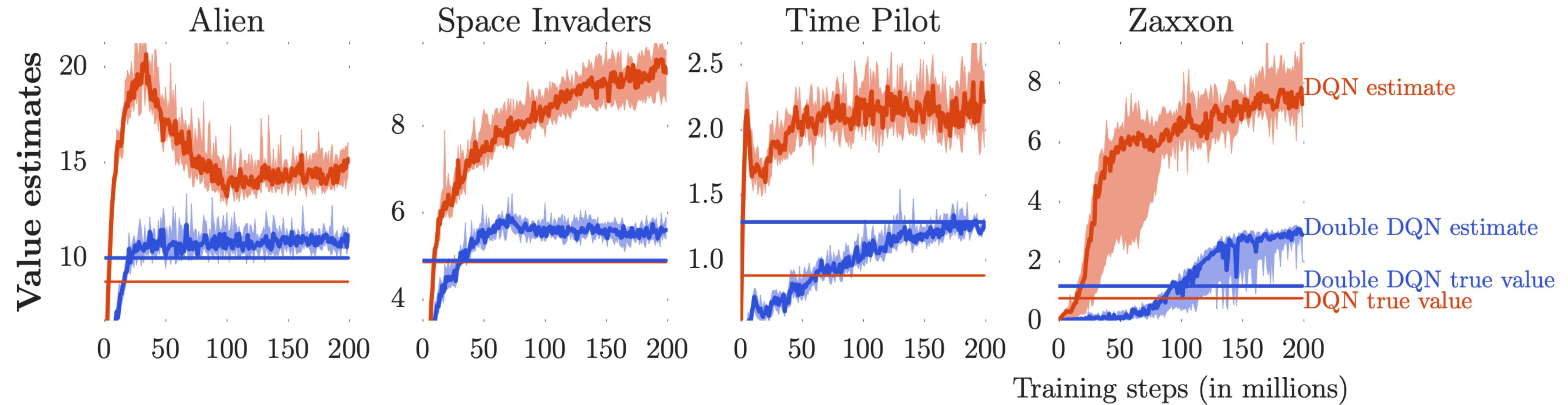
1st trick: Target Networks

Loss function of the Critic: MSBE (*Mean Squared Bellman Error*)

$$L(\phi, \mathcal{D}) = \underset{(s,a,r,s',d) \sim \mathcal{D}}{\text{E}} \left[\left(Q_\phi(s, a) - y(r, s', d) \right)^2 \right]$$

$$y(r, s', d) = R(s, a, s') + \gamma(1 - d) \left(Q_{\phi_{targ}}(s', \tilde{a}') - \alpha \log \pi(\tilde{a}' | s') \right) \quad \text{avec} \quad \tilde{a}' \sim \pi_\theta(\cdot | s')$$

Critic

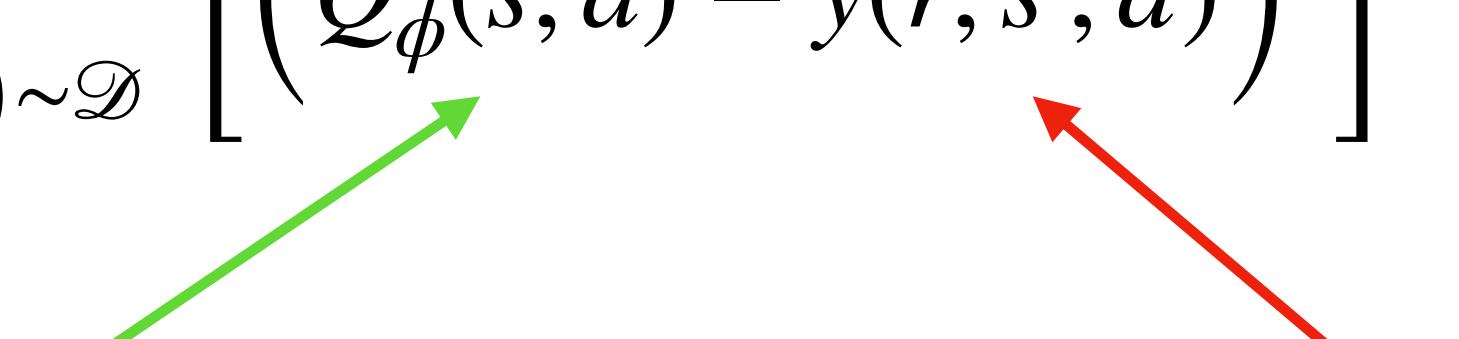


Source: Deep Reinforcement Learning with Double Q-learning (Hasselt et al., 2015)

Critic

1st trick: Target Networks

Loss function of the Critic: MSBE (*Mean Squared Bellman Error*)

$$L(\phi, \mathcal{D}) = \underset{(s,a,r,s',d) \sim \mathcal{D}}{\text{E}} \left[\left(Q_\phi(s, a) - y(r, s', d) \right)^2 \right]$$


$$y(r, s', d) = R(s, a, s') + \gamma(1 - d) \left(Q_{\phi_{targ}}(s', \tilde{a}') - \alpha \log \pi(\tilde{a}' \mid s') \right) \quad \text{avec} \quad \tilde{a}' \sim \pi_\theta(\cdot \mid s')$$

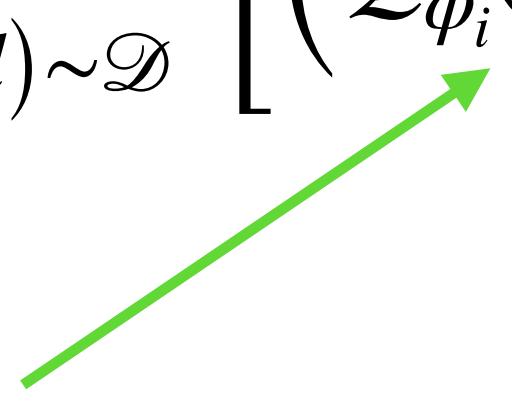
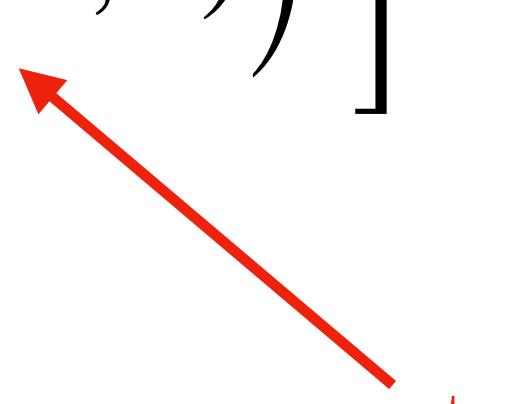
Critic

2nd trick: Clipped Double Q-network $\rightarrow \phi_1$ and ϕ_2

Loss function of the Critic: MSBE (*Mean Squared Bellman Error*)

For $i = 1, 2$:

$$L(\phi_i, \mathcal{D}) = \mathbb{E}_{(s, a, r, s', d) \sim \mathcal{D}} \left[\left(Q_{\phi_i}(s, a) - y(r, s', d) \right)^2 \right]$$

approximator  target 

$$y(r, s', d) = R(s, a, s') + \gamma(1 - d) \left(\min_{j=1,2} Q_{\phi_{\text{targ}, j}}(s', \tilde{a}') - \alpha \log \pi(\tilde{a}' | s') \right) \quad \text{avec } \tilde{a}' \sim \pi_\theta(\cdot | s')$$

Actor

$$\pi^* = \arg \max_{\pi} V^\pi(s)$$

Objective function of the Actor for each state s:

$$V^\pi(s) = \mathbb{E}_{a \sim \pi} [Q^\pi(s, a) - \alpha \log \pi(a \mid s)]$$

Actor

$$\pi^* = \arg \max_{\pi} V^\pi(s)$$

Objective function of the Actor for each state s:

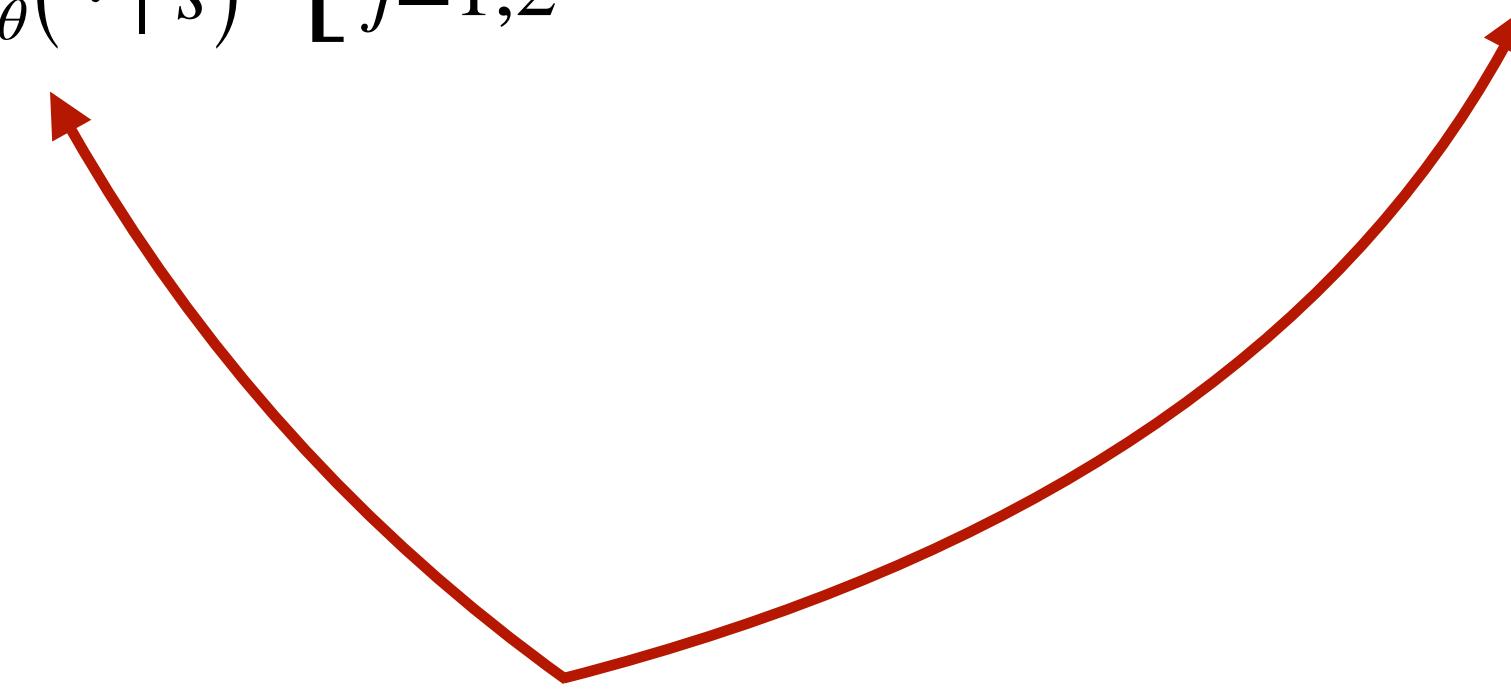
$$V^\pi(s) = \mathbb{E}_{\tilde{a} \sim \pi_\theta(\cdot | s)} \left[\min_{j=1,2} Q_{\phi_{\text{targ},j}}(s, \tilde{a}) - \alpha \log \pi_\theta(\tilde{a} | s) \right]$$

Actor

$$\pi^* = \arg \max_{\pi} V^\pi(s)$$

Objective function of the Actor for each state s:

$$V^\pi(s) = \mathbb{E}_{\tilde{a} \sim \pi_\theta(\cdot | s)} \left[\min_{j=1,2} Q_{\phi_{\text{targ},j}}(s, \tilde{a}) - \alpha \log \pi_\theta(\tilde{a} | s) \right]$$



Pain point: the distribution depends on policy params

Actor

3rd Trick : reparameterization

Objective function of the Actor for each state s:

$$V^\pi(s) = \underset{\xi \sim \mathcal{N}}{\text{E}} \left[Q^{\pi_\theta} (s, \tilde{a}_\theta(s, \xi)) - \alpha \log \pi_\theta (\tilde{a}_\theta(s, \xi) \mid s) \right]$$

$$\tilde{a}_\theta(s, \xi) = \tanh (\mu_\theta(s) + \sigma_\theta(s) \odot \xi), \quad \xi \sim \mathcal{N}(0, I)$$

Actor

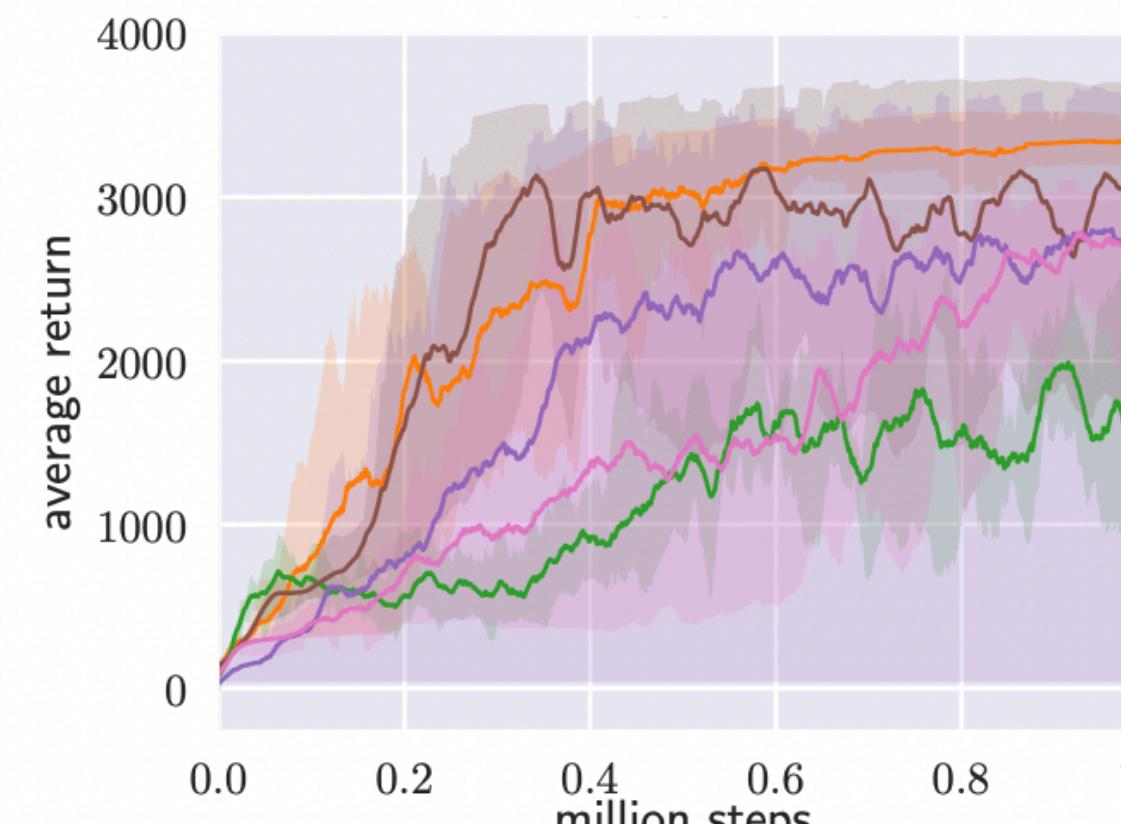
3rd Trick : reparameterization

Objective function of the Actor:

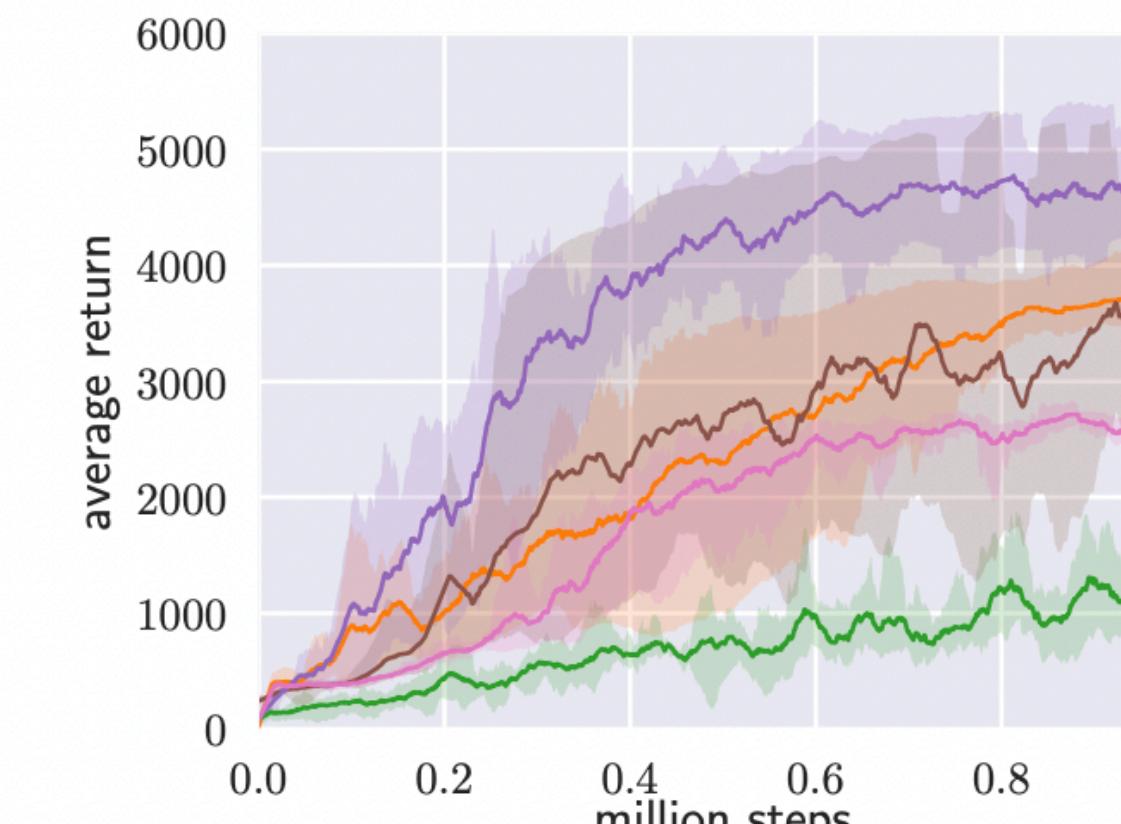
$$\max_{\theta} \mathbb{E}_{\substack{s \sim \mathcal{D} \\ \xi \sim \mathcal{N}}} \left[\min_{j=1,2} Q_{\phi_j}(s, \tilde{a}_\theta(s, \xi)) - \alpha \log \pi_\theta(\tilde{a}_\theta(s, \xi) \mid s) \right]$$

$$\tilde{a}_\theta(s, \xi) = \tanh(\mu_\theta(s) + \sigma_\theta(s) \odot \xi), \quad \xi \sim \mathcal{N}(0, I)$$

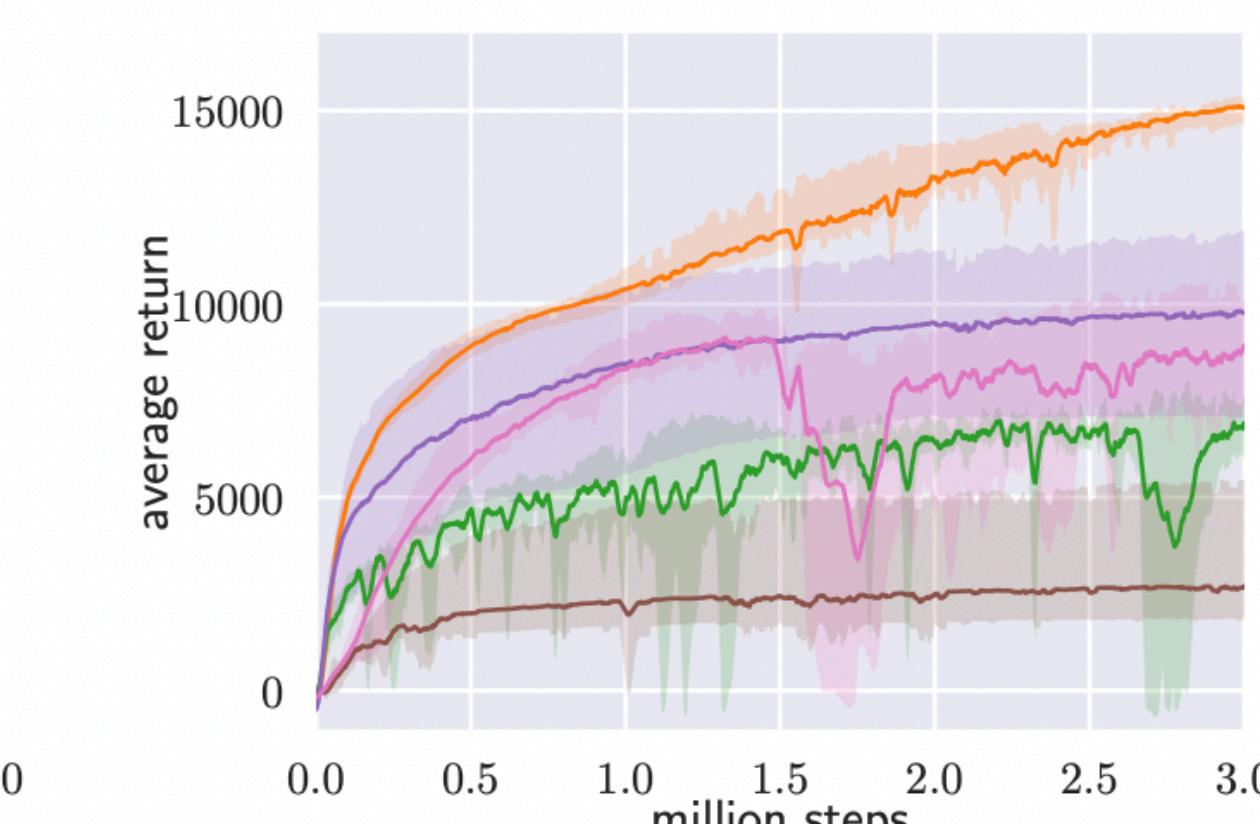
Results



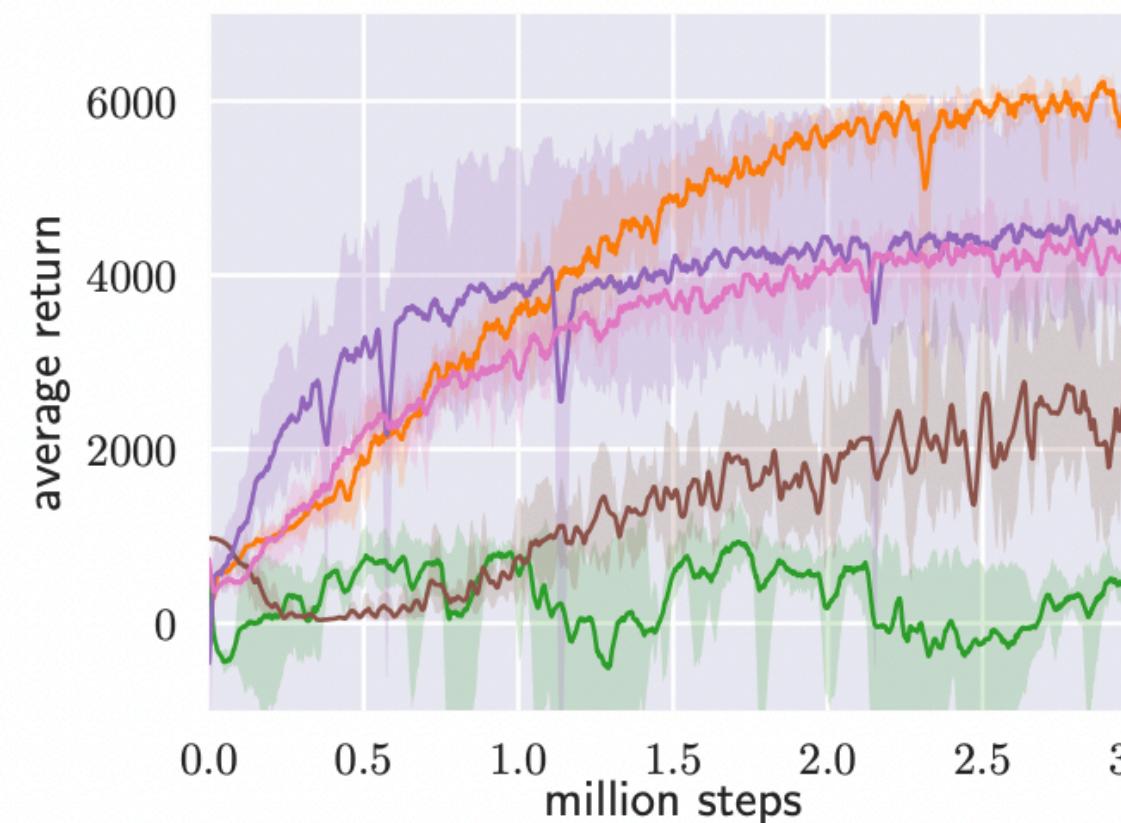
(a) Hopper-v1



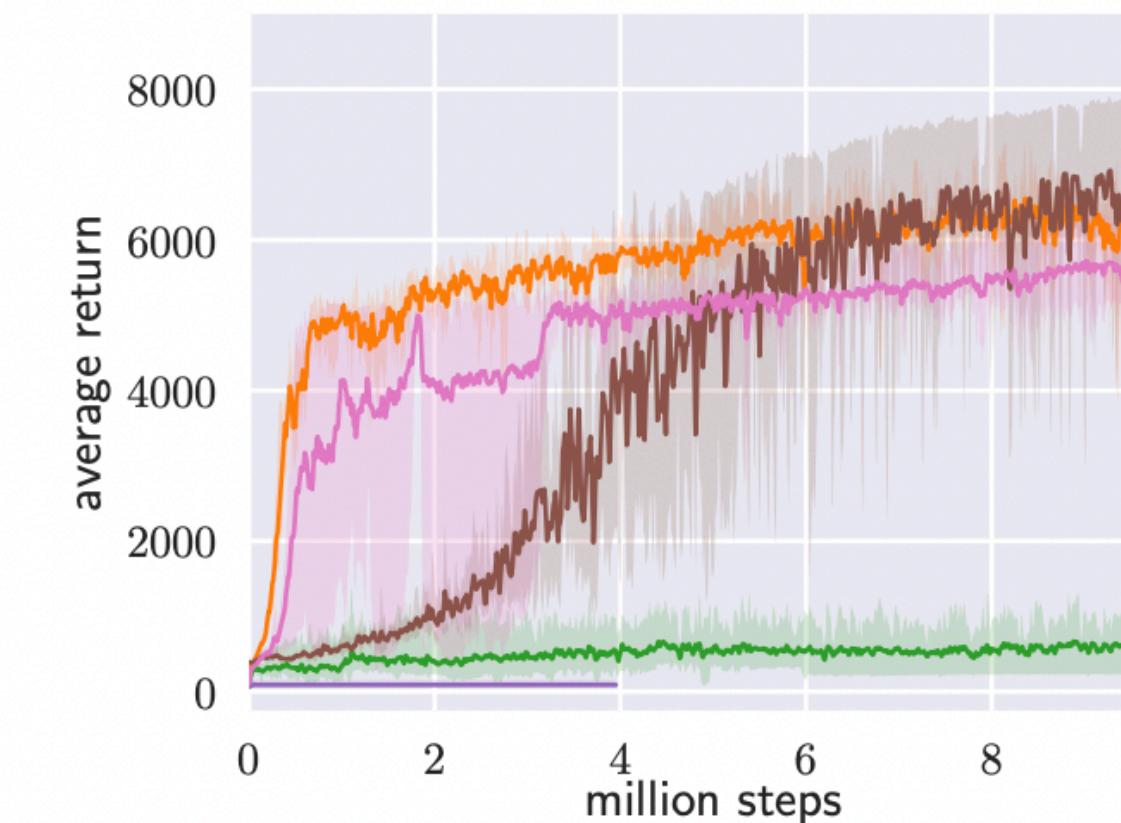
(b) Walker2d-v1



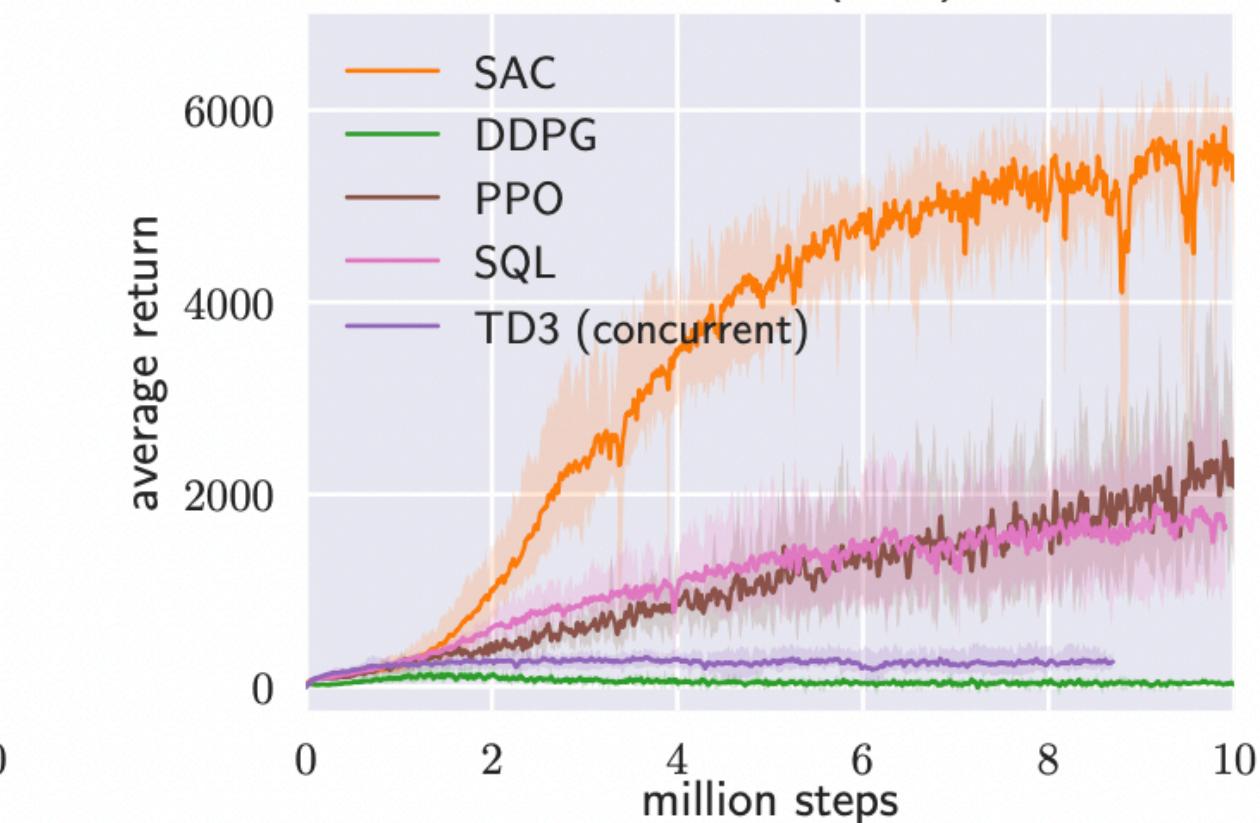
(c) HalfCheetah-v1



(d) Ant-v1



(e) Humanoid-v1



(f) Humanoid (rllab)

References

- Haarnoja, Tuomas, et al. "Soft actor-critic: Off-policy maximum entropy deep reinforcement learning with a stochastic actor." *International conference on machine learning*. PMLR, 2018.
- Silver, David, et al. "Deterministic policy gradient algorithms." *International conference on machine learning*. PMLR, 2014.
- Fujimoto, Scott, Herke Hoof, and David Meger. "Addressing function approximation error in actor-critic methods." *International conference on machine learning*. PMLR, 2018.
- <https://spinningup.openai.com/en/latest/algorithms/sac.html>